Forwarding in a Content-Based Network

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ABSTRACT

This paper presents an algorithm for content-based forwarding, an essential function in content-based networking. Unlike in traditional address-based unicast or multicast networks, where messages are given explicit destination addresses, the movement of messages through a content-based network is driven by predicates applied to the content of the messages. Forwarding in such a network amounts to evaluating the predicates stored in a router's forwarding table in order to decide to which neighbor routers the message should be sent. We are interested in finding a forwarding algorithm that can make this decision as quickly as possible in situations where there are numerous, complex predicates and high volumes of messages. We present such an algorithm and give the results of studies evaluating its performance.

Categories and Subject Descriptors

C.2.2 [Computer-Communication Networks]: Network Protocols—*Routing protocols*; C.2.1 [Computer-Communication Networks]: Network Architecture and Design—*Distributed networks*; C.2.4 [Computer-Communication Networks]: Distributed Systems—*Distributed applications*

General Terms

Algorithms, Measurement, Performance, Experimentation

Keywords

Content-based network, forwarding, matching, overlay, publish/subscribe $% \mathcal{A} = \mathcal{A} = \mathcal{A} + \mathcal{A}$

1. INTRODUCTION

Content-based communication is a novel communication service whereby the flow of messages from senders to receivers is driven by the content of the messages, rather than by explicit addresses assigned by senders and attached to the

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messages [9]. Using a content-based communication service, receivers declare their interests by means of *selection predicates*, while senders simply publish messages. The service consists of delivering to any and all receivers each message that matches the selection predicates declared by those receivers.

In a content-based service model, message content is structured as a set of attribute/value pairs, and a selection predicate is a logical *disjunction* of *conjunctions* of elementary *constraints* over the values of individual attributes. For example, a message might have the following content

[class="alert", severity=6, device-type="web-server", alert-type="hardware failure"]

which would match a selection predicate such as this:

[alert-type="intrusion" \land severity>2 \lor class="alert" \land device-type="web-server"]

An ideal application for a content-based communication service is a publish/subscribe event notification service [4, 5, 7], where a selection predicate represents a subscription and a message represents a published event. Other applications that can directly benefit from a content-based communication service include system monitoring and management, network intrusion detection, service discovery, data sharing, distributed electronic auctions, and distributed games.

We believe that the best way to provide a contentbased communication service is through a content-based network. A content-based network is an overlay network whose routers perform specialized routing and forwarding functions. Routing in a content-based network amounts to synthesizing distribution paths from a combination of the topological features of the overlay network and the selection predicates declared by applications. The routing function compiles two forwarding tables: the first contains topological constraints, and is conceptually identical to a forwarding table of an IP router, while the second contains selection predicates, and is the result of combining the selection predicates declared by applications. The forwarding function determines the set of next-hop destinations by applying the appropriate topological constraints found in the first table, and by matching the content of the message against the set of selection predicates found in the second table.

Our concern in this paper is with the design of a fast forwarding function for a content-based network. In particular, we focus on the predicate-matching algorithm, since this is the novel aspect of the forwarding function in a contentbased network. Notice that the properties of the forwarding table used by this algorithm (the second table mentioned

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above) result directly from the characteristics of end-user applications, as opposed to characteristics of the network itself. We seek an algorithm that can scale well in situations where there are numerous, complex predicates and high volumes of messages generated by end-user applications.

In this paper we present a forwarding algorithm and give the results of studies evaluating its performance. Because our goal is *fast* forwarding, our primary metric for success is how well we minimize, for a given message, the time it takes to identify the set of neighbors to which the message should be forwarded. Intuitively, the main scale factor of the algorithm is the total number of constraints resident in the forwarding table.

Our evaluation shows that the algorithm has good absolute performance under heavy loads and in a variety of network configurations, including the extreme case of a single, centralized router. It also shows that the algorithm scales sublinearly in the number of conjunctions, with almost no degradation of throughput, in the context of a network of routers with a fixed number of neighbor nodes. For example, a software implementation of our algorithm, running on a 950Mhz computer, is able to forward a 10-attribute message in 3 milliseconds in a situation where there are 20 predicates (i.e., neighbors) consisting of 250000 conjunctions formed from 5 million individual constraints over an alphabet of 1000 attributes. In this experiment, the message went to 18 of the 20 neighbors, but we observed in other experiments that the performance generally improves (i.e., the forwarding time goes down) as the percentage of matching neighbors goes down. In terms of space, the forwarding table in this experiment occupies only 48 bytes per constraint, even though we have not yet turned our attention to optimizing that aspect of the algorithm.

In the next section we provide some necessary detail concerning the content-based service model and the general architecture of a content-based network. We then discuss related work, highlighting the contribution of this paper. Following that, we present our forwarding algorithm. An experimental evaluation of its performance is then described. We conclude with a summary and future plans.

2. CONTENT-BASED NETWORKING

A content-based network is an application-level overlay consisting of client nodes and router nodes, connected by communication links. A content-based network accepts messages for delivery, and is connectionless and best-effort in nature. As mentioned in the previous section, it is the communication model of a content-based network that differs significantly from a traditional (unicast or multicast) address-based network such as IP. In a content-based network, nodes are not assigned unique network addresses, nor are messages addressed to any specific node. Instead, each node advertises a *predicate* that defines messages of interest for that node and, thus, the messages that the node intends to receive. The content-based service consists of delivering a message to all the client nodes that advertised predicates matching the message.

The content-based service does not eliminate the need for network addresses. Instead, it limits their use to that of node identifiers. In particular, node identifiers are needed to associate predicates with their issuers, to maintain topological routing information, and to manage direct (lower-level) communications between nodes. The fundamental difference with respect to traditional networks such as IP is that these identifiers are not used as locators or destination specifiers by either senders or receivers.

The concept of a content-based network service is independent of the form of messages and predicates. Denoting the universe of messages as \mathcal{M} , and the universe of predicates over \mathcal{M} as $\mathcal{P} : \mathcal{M} \to \{true, false\}$, we say that \mathcal{P} and \mathcal{M} define a *content-based addressing scheme*, which in turn defines the content-based service. Consistently we say that the predicate p_n advertised by n is the *content-based address* of the node n. We also say that a message m is implicitly addressed by its content to a node n with content-based address p_n if $p_n(m) = true$.

In practice, we must refine these definitions somewhat. Here we use the concrete syntax and semantics embodied in the Siena event notification service [7] to illustrate what we mean by messages and predicates. Thus, a message is a set of typed attributes. Each attribute is uniquely identified within the message by a *name*, and has a *type* and a value. For purposes of this paper, we consider the common types string, integer, and boolean. For example, [string carrier = UA; string dest = ORD; int price = 300; bool upgradeable = true;] would be a valid message. A predicate is a disjunction of conjunctions of constraints on individual attributes. Each constraint has a name, a type, an operator, and a *value*. A constraint defines an elementary condition over a message. A message matches a constraint if it contains an attribute with the same name and type, and if the value matches the condition defined by the operator and value of the constraint. For example, [string dest = $ORD \land$ int price < 400] is a valid predicate matching the message of the previous example.

Note that the service model of Siena is largely consistent with other publish/subscribe services [4, 5, 12, 16, 19, 21]. The choice of a disjunctive normal form for predicates is also a natural extension of existing standards for applicationlevel publish/subscribe services (e.g., JMS and Corba NS), in which multiple subscriptions are combined naturally to form summary predicates that are disjunctions of the elementary subscriptions. To date we have not considered the pros and cons of an alternative content-based addressing scheme based on a conjunctive normal form of predicates.

2.1 Content-Based Routing

In order to put the forwarding function in context, we briefly describe the routing scheme that is used in conjunction with the forwarding function. Details of the routing scheme are presented elsewhere [8].

At a high level we propose to implement a content-based network service starting from the basis of a broadcast system, and then using advertised predicates to prune branches of the broadcast distribution trees, thereby limiting the propagation of each message to only those nodes that advertised predicates matching the message. This strategy is illustrated in Figure 1. To implement this routing scheme, a router runs two types of routing protocols: a *broadcast routing* protocol and a *content-based routing* protocol. The first protocol processes topological information and maintains the forwarding state that would be necessary to implement a broadcast system. The second protocol processes predicates advertised by nodes, and maintains the forwarding state necessary to decide, for each router interface, whether a message matches the predicates advertised by any down-



content-based "physical" overlay

Figure 1: Network Overlay and High-Level Routing Scheme

stream node reachable through that interface. (Notice that, by analogy to an IP network, we term the connections of a content-based router to its adjacent nodes as the *interfaces* of that router.)

The content-based routing protocol uses two mechanisms for the propagation of routing information. The first is a "push" mechanism based on *receiver advertisements*, while the second one is a "pull" mechanism based on *sender requests* and *update replies*.

Receiver advertisements (RAs) are issued by nodes periodically and/or when they advertise new content-based addresses. An RA carries the content-based address as well as the identifier of its issuer, and its purpose is to push routing information from the issuer (receiver) out to all the potential senders. The propagation of an RA follows the broadcast tree rooted at the issuer node, and sets up reverse forwarding paths towards the issuer. Specifically, at each node, the predicate advertised by an RA is added (i.e., combined in a logical disjunction) to the predicate associated with the interface that is on the reverse path to the issuer. If this logical combination generates a new predicate for that interface, then the node continues the propagation of the RA. Otherwise, the node simply stops propagating the RA. Notice that by pruning the propagation of RAs in this latter case, content-based routers avoid advertising content-based addresses along paths that are already set up with the necessary forwarding state. Notice also that, by the same pruning rule, RAs can only "widen" the selection of content-based addresses in routing tables. This effect is balanced by the use of sender requests.

A router uses a sender request (SR) to collect routing information from other routers. SRs are issued on a regular basis by each node, and are designed to pull contentbased routing information from receivers back to senders. An SR flows from its issuer to every other node, following the broadcast tree rooted at the issuer. Routers respond to SRs by generating update replies (URs). URs are returned back to the issuer of the SR, on the reverse path of the SR, accumulating content-based addresses along the way. Specifically, leaf nodes immediately return a UR containing their content-based address. Intermediate nodes compute

	f _{1.1}	string dest = int price < 500
I_1	f _{1.2}	$\begin{array}{ccc} string & stock = DYS\\ int & quantity > 1000\\ int & price < 500 \end{array}$
	f _{2.1}	string airline = UA string orig = Chicago string dest = Atlanta
I_2	f _{2.2}	string dest = New York int price < 200
	f _{2.3}	string orig = Chicago
	$f_{2.4}$	string $airline = UAbool$ $upgradeable = true$
I_3	f _{3.1}	string stock = MSFT int price < 200

Figure 2: Example Contents of a Forwarding Table

their UR by combining (in a logical disjunction) their own content-based address with the content-based addresses reported by the URs received from routers downstream from the issuer. Eventually, the issuer of the SR receives one UR per interface, each one carrying the combined content-based address of the nodes reachable through that interface.

2.2 Content-Based Forwarding and Problem Statement

Following the routing scheme described above, we propose a forwarding process consisting of the combination of *broadcast forwarding* and *content-based forwarding*. In this paper we focus on the design of the content-based forwarding algorithm and assume the availability of a generic broadcast forwarding function.

Without loss of generality, we assume that the output of the given broadcast forwarding function for a message m originating at a node s is a set of output interfaces B. For example, with a broadcast protocol that uses minimal source-based trees, B is the set of links downstream on the directed, shortest-paths spanning tree rooted in s, whereas with reverse-path broadcast forwarding [10] B is the complete set of interfaces of the router when m is received over the link that is on the (reverse) unicast path to s.

We also assume that the content-based routing protocol maintains a *content-based forwarding table*. The table represents a map between interfaces and predicates, where a predicate p_i associated with interface *i* represents the union of the predicates advertised by downstream nodes reachable through *i* or, in general, a superset thereof. Figure 2 shows an example of a content-based forwarding table (the details of this table are explained in Section 4).

Given this modularization of the broadcast routing and forwarding functions, and of the content-based routing function, we define content-based forwarding as a function CBFof three inputs: a message m, a set of broadcast output interfaces B, and a content-based forwarding table $T = \{p_1, p_2, \ldots, p_I\}$, where I is the total number of interfaces. The function computes the subset of the broadcast output B that includes all the interfaces in T associated with a predicate matched by m. Formally:

 $CBF(m, B, T) = \{i : i \in B \land matches(p_i, m)\}$

Our goal is to design a fast algorithm for CBF.

3. RELATED WORK AND CONTRIBU-TIONS OF THIS PAPER

In order to place our work within the proper context, we first discuss the concept of content-based networking in relation to other research efforts in the general area of advanced network services, and then relate our proposed algorithm to other forwarding and matching algorithms.

IP Multicast. Content-based networking can be seen as an extension of a multicast network service such as IP multicast [11]. The two service models are similar in that they both allow senders and receivers to communicate indirectly through a logical rendezvous point, but differ significantly in their flexibility. Formally, this difference can be characterized as follows: the multicast model allows senders and receivers to create and refer to *partitions* of the information space, while the content-based model allows senders to use a completely open information space, and receivers to select information from *arbitrary subsets* of that space. In practice, this means that the IP multicast service is well suited to streaming media, where information is channeled in a relatively small number of groups, and where group members are interested in receiving everything that is sent to the group. Conversely, content-based networking is intended to better support distributed applications, where application components need fine-grained selection of the information they exchange. This view of the IP multicast model and the difference between it and the content-based model have also been pointed out elsewhere [9, 15].

Extended Multicast Models. Stoica et al. [18] have proposed the internet indirection infrastructure (i3), as a platform to implement various forms of advanced network services, including multicast, anycast, and mobility. The service model of i3 provides a rendezvous-based communication service similar to that of IP multicast, but with an extended "join" semantics. Clearly, i3 and our content-based networking model have similar goals, in that they are intended to better support advanced distributed applications. However, they are based on rather different design decisions: i3 uses a single identifier as a logical rendezvous point, whereas our content-based model uses structured information and more powerful selection predicates.

Content-Addressable Network and Content Routing. Despite the similarity in terminology, the content-based networking model presented in this paper has practically no relationship to the model of content-addressable network proposed by Ratnasamy et al. [17]. As they use it, the term "content-addressable network" indicates what amounts to a lookup service that maps keys (usually resource identifiers such as file names) to keys (usually locations). Another work that uses similar terminology is that of Gitter and Cheriton [13]. Gitter and Cheriton propose a "content routing" scheme whereby names of resources are pushed into the network, and where some routers are capable of forwarding packets based on the name of the destination resource. This content routing service model is quite different from our content-based service in both goals and functionality.

Packet Classification. Some applications, including intrusion detection systems, firewalls, and differentiated services, require routers to make forwarding decisions based on an extended set of header fields, or even payload data. This decision process, also called packet classification, has been studied extensively and admits fast solutions [3]. The algorithms developed for packet classification, however, are applicable only to a reduced subset of our content-based forwarding problem. The reason for this incompatibility is twofold. Firstly, in packet classification, the selection is made by looking up a limited set of predefined fields. This gives these algorithms direct access to the values of fields of interest, and also allows them to construct specialized indexes for their specific data types. Conversely, messages in a content-based network have a less rigid structure, consisting of arbitrary sets of attributes in which each attribute is identified by its name. This requires an additional search process and more conservative matching strategies. Secondly, existing packet classification algorithms are unicast in nature, whereas content-based forwarding is inherently multicast.

Intentional Naming. The idea of content-based networking is also related to the idea of an intentional naming system (INS) proposed by Adjie-Winoto et al. [1]. With INS, a server announces its services with an "intentional" name, while a client addresses a message to a server with a query that specifies the desired properties of the service. INS can act both as a name-resolution service or a "late-binding" delivery service. In the first case, INS returns a set of IP addresses, while in the second case, INS forwards the message to any one or all the servers it finds.

One significant difference between the INS model and our content-based model is in the expressive power of names versus predicates. Names in INS are essentially an ordered conjunction of equality or "don't care" constraints. Instead, predicates in content-based networking are a disjunctive normal form (unordered disjunction of conjunctions) of a larger set of constraints, including inequality (<, >, and \neq) and string operators such as substring, prefix, and suffix, applicable to a richer set of types (strings, numbers, booleans). This difference has a significant impact on both the evaluation (forwarding) and propagation (routing) of predicates. We do not see how the architecture and algorithms proposed by Adjie-Winoto et al. can be adapted to the more expressive language of content-based networking.

Another difference is in the approach to routing and forwarding. INS is based on a single data structure to serve as both a forwarding and routing table. We believe that this approach has serious problems. In fact, we used this same approach in our design and implementation of the Siena publish/subscribe service, only to realize that, while conceptually simpler, it forces the use of data structures and algorithms that introduce unacceptable performance compromises for the forwarding function or the routing function, or both. Again, the separation of concerns for these two functions is an integral part of our current approach.

The general routing strategy is also a differentiator between our approach and INS. INS propagates intentional names everywhere, while our strategy is to limit the propagation of predicates using their semantic relations (see Section 2.1). Notice that this strategy is not applicable to INS because it conflicts with its name-resolution function. In fact, in order to be able to resolve names directly, every router in INS must maintain the name records for the entire network. SDI Problem. Yan and Garcia-Molina first suggested the idea of building indexes of predicates [20]. However, their context was quite different from ours. They were interested in better solutions to the SDI (selective dissemination of information) problem, which they characterize as finding the set of users interested in a document newly added to some collection of documents. An example application is a notification service for a digital library. The interests of users are represented by what are called *profiles*. The profiles are compared against a new document to determine a match. A document in this setting is treated as a set of words, and a profile is simply a conjunction of words. A profile matches a document if the document contains all the words in the profile. Yan and Garcia-Molina recognized that indexing the profiles (i.e., the predicates) could greatly speed up the matching function in the presence of large numbers of profiles. They developed a system called SIFT to demonstrate their ideas [21]. Yan and Garcia-Molina also describe an early prototype of a distributed service [21]. However, the purpose of that service is to offer increased reliability through replication, not act as a network of store-andforward routers.

Event Matching in Publish/Subscribe Systems. More recently, several researchers have studied the problem of evaluating a possibly large number of predicates against messagelike data (as opposed to a large document) in the domain of filter matching for publish/subscribe systems. For this problem, various forms of decision trees and indexing structures for subscriptions have been proposed. These efforts can be classified into two broad categories based on the strategy used to search the predicate space. The first approach is to start from the attribute constraints derived from the full set of subscriptions, and to move through them consulting the attributes appearing in the message. This approach is used in the form of a matching tree by Gough and Smith [14] and by Aguilera et al. [2]. It is also used in the form of a binary decision diagram by Campailla et al. [6]. The opposite approach is to start from the attributes of the message, and to move through them consulting the constraints. This is the approach used by Yan and Garcia-Molina in SIFT, if we consider a new document to be a "message" whose "attributes" are formed from the set of words appearing in the document. It is also the approach used by Fabret et al. in their publish/subscribe system Le Subscribe [12]. Le Subscribe goes beyond the SIFT indexing scheme by providing a main-memory matching algorithm that is "processor cache conscious", and by providing heuristic optimizations based on a clustering of subscriptions that share the same equality constraints over the same attributes.

Contributions. The work presented in this paper generally conforms to the second approach. We use the indexing data structure developed by Yan and Garcia-Molina as a starting point. In particular, we adopt their scheme for maintaining a global index of attribute constraints whose selection, based on the attributes of the input message, leads to the rapid identification of matching conjunctions. (Details are given in Section 4.) However, we have extended their ideas significantly, both to enhance the functionality of the matching algorithm and to make it appropriate for use in the forwarding function of a content-based network. The extensions include the following contributions.

- We extended the set of types and operators that can be used in predicates. SIFT is limited to strings (i.e., "words") and the equality operator over strings. Le Subscribe added integers and their associated relational operators. To this we have added the prefix, suffix, and substring operators for strings. These additional operators require the careful design and integration of whole new indexing structures.
- We added the explicit expression of disjunctions to the model of predicates.
- Given the presence of disjunctions, we developed a powerful optimization based on the construction of what we call a *selectivity table*. The table is used to summarize for each attribute in the alphabet of attributes, the subset of predicates for which those attributes are required for matching. For instance, in the predicate $(c_r \wedge c_s) \lor (c'_r \wedge c_t)$, where c_r and c'_r represent constraints on attribute r, and c_s and c_t represent constraints on attributes s and t, if the incoming message does not contain an attribute r, then we know immediately, without further processing, that the predicate cannot be matched. To give a flavor of the effectiveness of this optimization, our results for one set of experiments showed that for an alphabet of 1000 attributes used in 200000 predicates, we can eliminate 131000 of those predicates by examining just the first 10 of the 1000 entries in the table.

4. FORWARDING ALGORITHM

Recalling the definitions of Section 2, a forwarding table is a one-to-one association of *predicates* to *inter-faces*. A predicate is a disjunction of conjunctions of elementary *constraints*, and a constraint is a quadruple $\langle type, name, op, value \rangle$. For convenience in the following discussion we refer to conjunctions of constraints simply as *filters*. Thus, selection predicates are disjunctions over what we call filters.

An example of the logical content of a forwarding table is shown in Figure 2, where I_s is an interface and $f_{s,t}$ is a filter in the disjunction of filters associated with interface I_s . Constraints on individual attributes within a filter are shown in the third column of the table. Although not evident in this particular example, identical filters can in general be associated with more than one interface, just as identical constraints can be associated with more than one filter.

Forwarding an incoming message m amounts to computing the set of interfaces associated with a predicate matching m. Because each interface is associated with exactly one predicate, in the following discussion we use the terms interface and predicate interchangeably. The forwarding function that we have developed is an evolution of a basic matching algorithm, which in turn is founded on a particular index structure representing the forwarding table. This basic algorithm is known as the *counting algorithm*, and has been applied to the matching problem in the context of centralized publish/subscribe systems [12, 20]. These previous applications of the counting algorithm have only dealt with predicates that were conjunctions, not disjunctions.

In order to describe our extended version of the algorithm, we first give a high-level view of the structure of the forwarding table and then introduce a simple variant of the counting algorithm that handles disjunctions. This variant can



Figure 3: Representation of the Forwarding Table of Figure 2

exploit the presence of disjunctions to optimize the matching process somewhat. Further optimizations are described in sections 4.2 and 4.3.

4.1 Forwarding Table and the Extended Counting Algorithm

At a high level, the forwarding table is organized as a twopart, left-to-right structure. The left-hand side is an index of all the individual constraints found in all the predicates associated with all the neighbors of the content-based router. The outputs of the left-hand side (i.e., the individual constraints lying at the ends of index paths) are connected as boolean inputs to the right-hand side of the structure; if the algorithm arrives at a particular constraint after traversing the index, then the constraint has been found to be true for the message. The right-hand side implements a network of logical connections representing the conjunctions of constraints into filters and the disjunction of filters into the predicates of interfaces. Figure 3 shows a schematic view of that data structure for the example of Figure 2.

Notice that the forwarding table is constructed and used as a "dictionary" data structure. This means that it is optimized for the lookup operation, while modifications are handled by rebuilding the table as a whole. This design choice is based on the assumption that message traffic (i.e., lookup operations) will dominate over control traffic (i.e., modification operations). Notice also that modification operations can be appropriately buffered, and therefore performed at a manageable rate.

Based on this general data structure, the counting algorithm proceeds as follows. For a given message m, it iterates through the attributes a_1, a_2, \ldots, a_k of m. For each attribute a_i , it finds the constraints $c_{i,1}, c_{i,2}, \ldots, c_{i,n_i}$ matched by a_i using the left-hand-side index of the forwarding table. Then, iterating through all the matched constraints $c_{1,1}, c_{1,2}, \ldots, c_{1,n_1}, \ldots, c_{k,1}, c_{k,2}, \ldots, c_{k,n_k}$, it finds the matched filters using the right-hand-side boolean network.

```
proc counting_CBF(message m) {
map < filter, int > counters = \emptyset
set < interface > matched = \emptyset
foreach a in m {
   set < constraint > C = matching_constraints(a)
   foreach c in C {
     foreach f in c.filters {
       if f.interface \not\in matched {
          if f ∉ counters {
             counters := counters \cup \langle f, 0 \rangle
          }
          counters[f] := counters[f] + 1
          if counters[f] = f.size {
             output(m,f.interface)
             matched := matched \cup {f.interface}
             if |matched| = total_interface_count {
               return \} } } } }
```

Figure 4: Pseudocode of the Counting Algorithm

Figure 4 shows the counting algorithm in pseudocode. The algorithm uses two running data structures to maintain state during the matching process. The first structure is a table of counters (hence the name of the algorithm) for partially matched filters. The second data structure is a set containing the interfaces to which the message should be forwarded. For each constraint found through the constraint index, the algorithm increments the counter of all the filters linked from that constraint. When a counter associated with filter f reaches the total number of constraints linked to f, the filter is satisfied and the algorithm adds the interface linked from f to the set of matched interfaces.

The main difference between this extended counting algorithm and its more basic counterpart is that having disjunctions of filters allows us to use the set of matched interfaces to shortcut the evaluation of the filters. In particular, we can eliminate a lookup in the table of counters for all the filters linked to an interface that has already been matched. Moreover, as an additional shortcut, we can terminate the execution of the whole process for a message as soon as the set of matched interfaces contains the complete set of neighbor interfaces, since we know that further processing cannot provide any additional information. Notice that all the sets and set operations in the forwarding algorithm can be implemented very efficiently with bit vectors.

Our extended counting algorithm is really only the starting point for the optimizations leading to a fast forwarding algorithm. In the remainder of this section we describe two of those optimizations, each focusing on one of the two sides of the forwarding table. Evaluations of the effectiveness of the optimizations are provided in Section 5.

4.2 Multi-Operator Index

The index forming the left-hand side of the forwarding table is meant to speed up the process of finding the constraints that are satisfied by an attribute of an incoming message. Obviously, the first stage in the index should be based on the constrained attribute's name and type. In our implementation we use a straightforward combination of a standard ternary search trie (TST) for the strings representing attribute names, and then a simple switch on the type.

Once we have selected the right name and type, we use subindexes that exploit specific properties of each constraint operator. For example, indexing equality constraints is an immediate application of traditional indexes, since it is equivalent to indexing values. To index less-than constraints on integer attributes $(int, name, <, k_1)$, $(int, name, <, k_2)$, ..., $(int, name, <, k_n)$, we can simply maintain the constraints ordered according to their constant value (a sorted vector would suffice). Then, to find all the constraints matched by a value x, we simply walk through the index going from the bottom to the top, finding all the constraints with constant value greater than x. A similar structure can be used for greater-than constraints. Notice that this implementation of indexes for integer constraints is optimal, since the complexity of the search operation is on the order of the size of the output (i.e., the number of matching constraints) plus the complexity of an exact match search in a table that can be optimized using well-known searching techniques. Figure 5 depicts an index for integer constraints processed against a corresponding attribute in a message.



Figure 5: Example of Integer Constraint Indexing

As mentioned in Section 3, previous algorithms were designed without consideration of the prefix, suffix, and substring operators for strings. We could use the same approach for these operators as we do for the integer operators, namely to create and maintain a separate subindex for each. In fact, this was what we did in an earlier version of our algorithm. However, that approach is not optimal for strings, since it requires a potentially large number of comparisons. In order to support the fuller set of string operators with a very efficient index structure, we developed a *multi-operator index* for string constraints capable of supporting equality, less-than, and greater-than operators, as well as the prefix, suffix, and substring operators all in a single index. The basic skeleton of this index is a TST that we have extended in three ways.

- We added the capability of matching partial strings, which we use to represent prefix and substring constraints.
- We added a pair of "crown" lists, which we use to link the sequence of less-than and greater-than constraints inserted as leaves in the TST.

• We added a pair of backtrack functions that are necessary to move from a partial match to the (alphabetically) closest complete match, which we use to jump to the less-than and greater-than chains.

An example of this extended TST is depicted in Figure 6. In addition to the basic TST structure, we have two types of nodes, representing partial and complete matches, respectively. Nodes that represent partial matches link prefix (pf) and substring (ss) constraints. Nodes that represent complete matches link equals (=), less-than (<), greater-than (>), and suffix (sf) operators. Nodes representing complete matches are also cross linked through two singly-linked lists representing the chains of less-than and greater-than operators. They link every complete match node to the nearest less-than or greater-than constraint. The less-than chain is depicted in Figure 6 using a dashed line. For sake of clarity, only the less-than chain is shown.

The lookup function starts from the first character of the input string, and uses a slightly modified TST lookup subfunction. This subfunction recognizes partial matches along the path through the TST, in addition to final, complete matches. When a partial-match node is reached, the function returns the prefix constraint and/or the substring constraint associated with that partial match. The function also returns a pointer to the corresponding internal node and a pointer to the position reached within the input string. These two pointers can then be passed to the same lookup function to continue the search from the previous partial match node. At some point, this process will terminate, either because it cannot move forward in the TST and/or because it has reached the end of the input string. If the final node touched by the lookup process is a leaf node of the TST (i.e., if it contains the terminator character #), then the lookup function returns the corresponding equality, inequality, and suffix constraints. If the terminal node is not a leaf (i.e., if no complete match was found), then the lookup function backtracks to the two closest leaf nodes, one preceding and the other following the final node in alphabetical order. From a matching final node or from the closest matching nodes, the lookup function can immediately jump onto the less-than and greater-than chains, reaching one-byone all the matching less-than and greater-than constraints.

The lookup process is then repeated for each character of the input string, ignoring prefix, equality, less-than, and greater-than operators. This iteration allows us to identify all the substring and suffix constraints.

The complexity of the complete lookup function is on the order of l times the complexity of a TST search plus the size of the output—that is, O(l(log N+l)+|result|), where l is the length of the input string, and N is the number of strings in the TST.

4.3 Exploiting Attribute Selectivity

Intuitively, we can save time in processing a message if we can eliminate interfaces from consideration as soon as possible. Eliminating an interface can mean eliminating the evaluation of potentially many filters, and in turn, potentially many constraints. We can see that our counting algorithm already succeeds in doing this to a certain degree, by making use of the set of matched interfaces, as described in Section 4.1.

However, we can go further than this, based on the following reasoning. Let us call an attribute name a the de-



Figure 6: Extended TST that Implements a Multi-Operator Index for String Constraints

terminant attribute name for interface I, if every filter of I contains at least one constraint on a. Because filters are conjunctions, if a message does not contain an attribute a, then the message cannot possibly be forwarded through interface I and so can be ignored during the processing of the message. For example, in the forwarding table of Figure 2, "price" is a determinant for interfaces I_1 and I_3 , "stock" is a determinant for I_3 , and no other attribute name is a determinant for any other interface.

We use the concept of a determinant to pre-compute from the set of predicates what we call a *selectivity table*, which is a map that associates attribute names with the interfaces for which that attribute name is a determinant. Computing the selectivity table is straightforward, and amounts to computing the intersection of the attribute names of all the filters for each interface. Note that it would also be straightforward to combine the name with a type for the purpose of establishing selectivity, but to keep the presentation simple, we do not discuss this point.

When a message arrives, we can use the table to easily calculate—without incurring the cost of traversing the forwarding table—an initial set of interfaces that will not match the message. We perform this pre-processing step by iterating through the selectivity table, excluding all the interfaces associated with determinant attributes that are not present in the message. In the subsequent processing of the message, we use this set exactly in the same way we use the set of matched interfaces. In fact, we use a single set to annotate both excluded and already matched interfaces. The resulting algorithm is identical to the extended counting algorithm, except for the introduction of the selectivity processing step (Figure 7).

In order to maximize the effectiveness of the preprocessing, we sort the selectivity table in descending order by the cardinality of the set of excluded interfaces. This way the pre-processing function will always encounter the most selective names first. We parameterize the preprocessing function by the number of pre-processing *rounds*, by which we mean how far down the selectivity table the pre-processing function will traverse. With zero rounds, the selective forwarding algorithm reduces to the counting algorithm, since the selectivity table is ignored. As we increase the number of rounds we should see an increase in the number of interfaces determined to be safely ignored, which should in turn lead to a performance improvement. However, adding more and more pre-processing rounds, and thus going farther and farther down in the selectivity table, will add fewer and fewer additional interfaces, at the cost of more and more lookup operations on the message and set-union operations on the data structure. Therefore, we would expect to see a continuous decline in performance beyond a certain point. This is borne out by the experiments described in the next section.

5. EVALUATION

In order to evaluate our algorithm, we implemented it and studied its performance using a series of synthetic workloads derived from various combinations of predicates, interfaces, and messages. The experiments we conducted are intended to provide an initial exploration of the parameter space. The main parameter values chosen for those experiments were based on our experience with a particular class of applications of content-based networking, namely those using a

proc selectivity_CBF(m, B, T) {	<i>map<name< i="">, <i>set<interface>></interface></i> selectivity</name<></i>
$map < filter, int > counters := \emptyset$	<i>int</i> pre_processing_rounds
$set < interface > ifs_to_ignore := all_ifs - B$	
$ifs_to_ignore := ifs_to_ignore - pre_process(m)$	proc $pre_process(m)$ {
foreach a in m $\{$	$set < interface > result = \emptyset$
$set < constraint > C = matching_constraints(T,a)$	$int rounds = pre_processing_rounds$
for each c in C $\{$	foreach (a,s) in selectivity {
foreach f in c.filters {	\mathbf{if} rounds = 0
if f.interface \in ifs_to_ignore {	return result
$\mathbf{if} \ \mathbf{f} \not\in \mathbf{counters}$	rounds := rounds -1
counters := counters $\cup \langle f, 0 \rangle$	$\mathbf{if} \ \mathbf{a} \not\in \mathbf{m} \ \{$
counters[f] := counters[f] + 1	$\mathrm{result}:=\mathrm{result}\cup\mathrm{s}$
if $counters[f] = f.size \{$	$if result = total_interface_count$
$\mathbf{output}(\mathbf{m}, \mathbf{f}. \mathbf{interface})$	\mathbf{return} result
$ifs_to_ignore := ifs_to_ignore \cup {f.interface}$	} }
$if ifs_to_ignore = total_interface_count$	return result
$\mathbf{return} \left. \right\} \left. \right\} \left. \right\} \left. \right\}$	}
}	

Figure 7: Pseudocode of the Forwarding Algorithm with Selectivity Table and Pre-Processing

publish/subscribe communication pattern. In this section we present the results of our evaluation. $^{\rm 1}$

5.1 Experimental Setup and Parameters

We implemented our algorithm in C++ and ran all the experiments on a 950Mhz computer with 512Mb of main memory. In addition to the main algorithm and data structures, we created some auxiliary programs to generate parameterized loads of filters and messages. In particular, we have identified and used the parameters listed in Table 1. We performed all the experiments with 100 messages (M = 100), each one having between 1 and 19 attributes $(a_l = 1, a_h = 19, \text{ and an average } \overline{a} = 10).$

M	number of messages		
a_l, a_h	number of attributes per message, uniform in		
	$[a_l, a_h)$ range		
Ι	number of interfaces $(=$ number of predicates $)$		
f_l, f_h	number of filters per interface, uniform in $[f_l, f_h)$		
	range		
c_l, c_h	number of constraints per filter, uniform in		
	$[c_l, c_h)$ range		
D_a	distribution function for attribute names		
D_c	distribution function for constraint names		
D_t	distribution function for data types in both fil-		
	ters and messages		
D_{os}	distribution function for operators in string con-		
	straints		
D_{oi}	distribution function for operators in integer		
	constraints		
D_s	distribution function for string values in both		
	filters and messages		
D_i	distribution function for integer values in both		
	filters and messages		

Table 1: Scenario Definition Parameters

Roughly speaking, the primary measure of scalability is the "size" of the forwarding table, which is well characterized by the total number of elementary constraints $C \approx I \times \overline{f} \times \overline{c}$, where $\overline{f} = \frac{1}{2}(f_l + f_h - 1)$ and $\overline{c} = \frac{1}{2}(c_l + c_h - 1)$. We experimented with forwarding tables of up to five million constraints, distributed in various ways among filters, and filters among interfaces. Specifically, we fixed the range of constraints per filter, with $c_l = 1$ and $c_h = 10$, and we used different numbers of interfaces I and different ratios of filters per interface, maintaining $f_l = 1$ and varying f_h . The choice of a fixed range of constraints per filter, with an average of five constraints per filter, is based on practical considerations on the type of filters we expect to be posed by typical end users. The number of interfaces I gives an indication of the characteristics of a router, its position, and it role in the larger content-based network. The resulting total number of filters $F = I \times \frac{1}{2} f_h$ is a rough measure of the total size of the network in terms of nodes and end users, and therefore an important measure of scalability.

For attribute names, we experimented with a set of 1000 elements ($|D_a| = 1000$). In order to use realistic names, we composed our sample sets by selecting random words out of a common dictionary, and we weighted our set of names using a Zipf distribution. We then used the same set of words for both attributes in messages and constraints in filters (and therefore $D_c = D_a$). Notice that while this may be a simplification in defining the experiments, in fact it produces the most challenging scenarios for a forwarding algorithm. The reason is that having two completely overlapping sets of names maximizes the chances of having matching attributes and constraints. In the opposite, extreme case of two completely disjoint name sets (one for attributes, and one for constraints) there would be no matches at all, and the time complexity for the forwarding algorithm would be $O(\overline{a} \log C).$

For attribute values, we used a combination of dictionary values for strings and a range for integers. For strings, we compiled a list of words by extracting 1000 words from the dictionary. For integer values we used a range of 100 values. For both integers and strings, we used a uniform distribution to select values. We used the same distribution of string and integer values for both the values in messages and the values in constraints. Notice once again that having a uni-

¹Our implementation and workload generator are available on line at http://www.cs.colorado.edu/serl/cbn/forwarding/.

fied set of values increases the possibilities of having positive matches between constraints and attributes, thereby adding complexity to the matching process.

For attribute types and constraint types we used the same distribution D_t : 50% strings and 50% integers. For operators in integer constraints, the distribution D_{oi} was 60% equality, 20% less-than, and 20% greater-than. Finally, for operators in string constraints, the distribution D_{os} was 35% equality, 15% prefix, 15% suffix, 15% substring, 10% less-than, and 10% greater-than.

5.2 Basic Results

Figures 8 and 9 show a summary of the results of our experiments. The graphs show the matching time per message over the total number of constraints in the forwarding table, which ranges from a few hundred to over five million. Every graph shows pairs of curves, representing the cases with no selectivity table pre-processing rounds (r = 0) and with 10 rounds (r = 10), respectively.



Figure 8: Performance of the Forwarding Algorithm (Centralized Architecture)

Figure 8 represents the degenerate situation in which we model a centralized router, namely where the forwarding table has exactly one filter per interface. This is the worst case for our algorithm, yet its performance is arguably quite reasonable, taking only about 330 milliseconds to match a message in the presence of over five million constraints, corresponding to more or less one million filters and one million interfaces. The most important observation we make concerning the graph of Figure 8 is that our optimization based on the selectivity table is particularly effective in this extremely difficult case, achieving a reduction of matching time of up to 40%.

Figure 9 shows that the performance of the forwarding algorithm in scenarios more closely modeling a network of content-based routers, with a fixed number of interfaces, is significantly better, both in the absolute values and in the general sublinear behavior. Notice that in these cases, the curves with zero rounds are essentially indistinguishable from the corresponding ones with 10 rounds of preprocessing. On the one hand, this says that our optimization has no effect in configurations with a high ratio of filters per interface. This is not surprising, since in the presence of many filters for each interface, it becomes highly unlikely for an attribute name to be present in all the filters of an interface, thus reducing the overall selectivity of each individual



Figure 9: Performance of the Forwarding Algorithm (Distributed Architecture)

attribute. On the other hand, from the same observation, we can conclude that our optimization does not add measurable cost, even in cases in which the simple version of the algorithm is already extremely fast.

It would seem that a fundamental parameter in determining the behavior of the algorithm would be the ratio of filters to interfaces, maintaining a fixed total number of constraints (i.e., essentially a fixed number of filters, and a fixed forwarding table size). This intuition is confirmed by the results shown in Figure 10. The graph expresses very well the effect of handling disjunctions, and in particular, it shows that the forwarding algorithm performs at its best with very large disjunctions. On the left-hand side of Figure 10, we see once again the positive effect of excluding interfaces using the selectivity table.



Figure 10: Performance of the Forwarding Algorithm with a Varying Ratio of Filters per Interface

5.3 Sensitivity to the Number of Pre-Processing Rounds

The idea of using the selectivity table is to reduce the processing time by pre-selecting interfaces that can be safely ignored during the forwarding function. The exact amount of this reduction depends essentially on the combination of two independent factors. The first is the level of selectivity of each name, which is purely a characteristic of the predicate set. The second is the number of pre-processing rounds. As we point out in Section 4.3, the initial effect of adding rounds is to exclude more interfaces from the main processing function. However, after a certain point, this effect should fade due to the reduced selectivity of names farther down in the selectivity table, and because each round adds a certain processing cost that depends on the number of interfaces.



Figure 11: Cost/Benefit Analysis of the Pre-Processing Function with Varying Number of Rounds

The tension between cost and benefit of the pre-processing function is exemplified by the experimental results shown in Figure 11. The two curves represent the advantage of the pre-processing function as a (percentage) performance gain, over the simple counting algorithm. The curve that shows the highest advantage corresponds to the case of five million constraints. All the experiments are run over forwarding tables with one filter per interface. The experiments show that the pre-processing function becomes ineffective and ultimately a cost after 50 to 70 rounds. We performed all our other experiments using 10 rounds.

5.4 Network Effect

The experiments discussed above evaluate the performance of our forwarding algorithm, but only by examining an individual router. The question that arises is whether a true network of routers would out perform a single, centralized router under the same heavy workload. We can answer this question by comparing the end-to-end latency induced by the forwarding function in two different scenarios: the first with a single router, and the second with a combination of interconnected routers. In both cases we consider a total of one million filters formed from five million constraints, where each filter is associated with a distinct destination. Notice that this configuration represents the worst case for our optimizations, so we would expect the performance to be better in practice.

The first configuration corresponds to the curve for I = Ffrom Figure 8. In this case, the latency is about 350 milliseconds, which corresponds to the matching time of one run of the forwarding function over the complete set of filters. The second configuration can be obtained by connecting the destination nodes through a set of routers with a limited number of interfaces. Using routers with *I* interfaces, interconnected in an appropriate configuration, we can reach *H* destinations with at most $2 \log_I H$ hops. In our example, using routers with 20 interfaces, we can span the network in at most 12 hops, which would give a worst-case total latency of only about 40 milliseconds, as shown by the curve for I = 20 in Figure 9. This clearly demonstrates the viability of using a network of routers that uses an appropriately optimized forwarding function.

5.5 Summary of Evaluation

Our experiments have shown that our forwarding algorithm has good absolute performance and good cost amortization over a variety of loads. In particular, we found that:

- the basic *short-circuit evaluation* of filters greatly reduces processing time in the case where a single message may match a large number of filters;
- the use of the *selectivity table* improves the ability to short circuit the forwarding function, reducing the matching time up to 40% in the critical cases of routers with numerous interfaces and especially in the extreme case of centralized routers; and
- the use of the *selectivity table* has no measurable costs over the basic algorithm.

In summary, the selectivity table proved to reduce forwarding costs in the most critical cases, without adding any penalties in other cases in which the simple matching algorithm already offers good performance. We conclude from the evaluations that our forwarding algorithm is viable under heavy loads, and that the optimizations we proposed have significant, positive effects.

6. CONCLUSION

In this paper we have presented the first algorithm designed specifically for the implementation of the forwarding function of routers in a content-based network. The algorithm is based on earlier work in the area of centralized content filtering of both large documents and small messages. Our algorithm refines, adapts, and extends this work for use in a very different context. We formulated a variant of the counting algorithm that can handle disjunctive predicates, and developed optimizations targeted specifically at the disjunctions that are the semantics of network interfaces in a content-based network.

In order to evaluate the algorithm, we created an implementation and subjected it to a battery of synthetic workloads. From these experiments we found that the algorithm has good overall performance. The experiments also confirm the validity of our optimization techniques, and the stability of the algorithm even in circumstances that are suboptimal for the optimizations.

In the immediate future we plan to integrate our algorithm into our prototype content-based network architecture. As a natural progression of this work, we plan to attack the hard problem of routing in a content-based network. Using logical relations between predicates, we have already defined the basic concepts of content-based subnetting and supernetting, and we have implemented what amounts to a routing table. Using that as a basis, we plan to study and develop optimized data structures for routing, as well as efficient and robust routing protocols for content-based networks.

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