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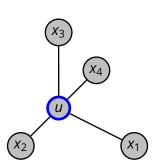
Outline

- Recap on link-state routing
- Distance-vector routing
- Bellman-Ford equation
- Distance-vector algorithm
- Examples

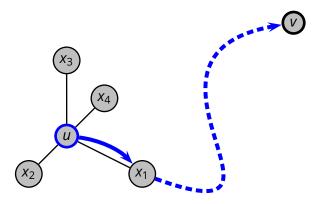














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- In essence
 - broadcast transmission of topology information
 - global knowledge of the network
 - local computation



Changes in Link Costs

- Routers monitor the state of their adjacent links
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 - e.g., measuring the round-trip time using a local "ping" protocol
- The measured costs are used to build LSAs, which are issued also at regular intervals
- Changes in link costs are propagated quickly to all routers
- Routers can then react by recomputing paths and by updating their forwarding tables accordingly
 - ▶ in fact, this "reaction" is not different from the normal behavior of the protocol



- Every router *u* maintains a "distance vector"
 - v is a destination node in the network
 - $\triangleright D_u[v]$ is the best known distance between u and v
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- If the distance vector of a neighbor leads to a better path to some destinations, the router updates its distance vector and sends it out again to its neighbors
- After a number of iterations, the algorithm converges to a point where every router has a minimal distance vector



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- Global computation
 - the computation is actually distributed



Intuition

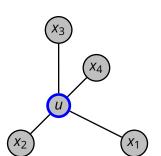
■ The main idea behind the distance-vector algorithm is expressed well by the Bellman-Ford equation

$$D'_{u}[v] = \min_{x \in neighbors(u)} (c(u, x) + D_{x}[v])$$

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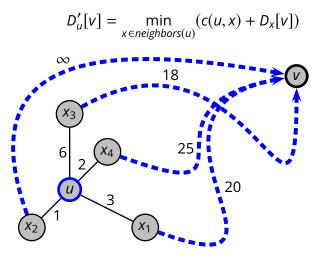
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 - ▶ $D_u[v]$, cost of the least-cost path from u to v (distance vector)
 - ▶ $n_u[v]$, next-hop node (neighbor of u) on the least-cost path from u to v
 - ► $D_x[v]$, distance vectors of every neighbor node x

Distance-Vector Algorithm: Initialization

Distance-Vector Algorithm: Loop

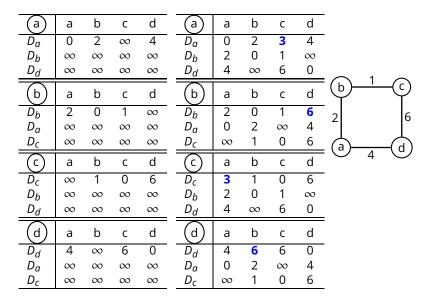
```
when D'_{x} is received from neighbor x
           do D_x \leftarrow D'_x
               for v \in N
                    do D_u[v] \leftarrow \min_{x \in neighbors(u)} (c(u, x) + D_x[v])
 5
               if D_{ij} was updated
 6
                  then send D_{ij} to all neighbor nodes
     when link cost c(u, x) changes
 8
           do for v \in N
                    do D_u[v] \leftarrow \min_{x \in neighbors(u)} (c(u, x) + D_x[v])
               if D_{ij} was updated
10
11
                  then send D_{ij} to all neighbor nodes
```

Distance-Vector Algorithm: D_u Update



a	а	b	С	d
Da	0	2	∞	4
D_b^{α}	∞	∞	∞	∞
D_d	∞	∞	∞	∞
b	а	b	С	d
D _b D _a	2	0	1	∞
D_{α}	∞	∞	∞	∞
D_{C}	∞	∞	∞	∞
_				
(n)	а	b	C	d
D_c	a ∞	b 1	с 0	d 6
D_c	∞	1	0	6
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $	∞ ∞	1 ∞	0 ∞	6 ∞
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $	∞ ∞ ∞	1 ∞ ∞	0 ∞ ∞	6 ∞ ∞
D_c D_b D_d	∞ ∞ ∞	1 ∞ ∞	0 ∞ ∞	6 ∞ ∞





a	b	C	d	(a)	а	b	C	d	(a)	а	b	C	d
0	2	∞	4	Da	0	2	3	4	Da	0	2	3	4
∞	∞	∞	∞	D_b	2	0	1	∞	D_b	2	0	1	6
∞	∞	∞	∞	D_d	4	∞	6	0	D_d	4	6	6	0
а	b	С	d	b	а	b	С	d	b	а	b	С	d
2	0	1	∞	D_b	2	0	1	6	D_b	2	0	1	6
∞	∞	∞	∞	D_{a}	0	2	∞	4	D_{a}	0	2	3	4
∞	∞	∞	∞	D_{C}	∞	1	0	6	D_{c}	3	1	0	6
а	b	С	d	<u>C</u>	а	b	С	d	<u>C</u>	а	b	С	d
∞	1	0	6	D_{c}	3	1	0	6	D_{c}	3	1	0	6
∞	∞	∞	∞	D_b	2	0	1	∞	D_b	2	0	1	6
∞	∞	∞	∞	D_d	4	∞	6	0	D_d	4	6	6	0
а	b	С	d	d	а	b	С	d	d	а	b	С	d
4	∞	6	0	D_d	4	6	6	0	D_d	4	6	6	0
∞	∞	∞	∞	D_{α}	0	2	∞	4	D_{α}	0	2	3	4
∞	∞	∞	∞	D_{c}	∞	1	0	6	D_{c}	3	1	0	6
	0	0 2 \\ \times \times \times \times \\ \times \times \times \\ \times \times \times \times \\ \times \times \times \times \times \times \\ \times \times \times \times \times \times \\ \times \times \times \times \times \times \times \\ \times \times \times \times \times \times \times \\ \times \times \times \times \times \times \times \times \\ \times \\ \times \ti	0 2 ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞	0 2 ∞ 4 ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞ ∞	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								

Example (2)



Example (2)

a	а	b	С	d
Da	0	2	∞	4
D_b	∞	∞	∞	∞
D_d	∞	∞	∞	∞
b	а	b	С	d
D_b	2	0	1	∞
D_a	∞	∞	∞	∞
D_{C}	∞	∞	∞	∞
<u> </u>	а	b	С	d
D_{c}	∞	1	0	9
D_b	∞	∞	∞	∞
D_d	∞	∞	∞	∞
D_a	α	~	ω	~
d	a	b	c	d
d				
D_d D_a	а	b	С	d
d	a 4	b ∞	c 9	d 0



Example (2)

(a)	а	b	С	d	(a)	а	b	С	d	_
Da	0	2	∞	4	Da	0	2	3	4	_
D_b	∞	∞	∞	∞	D_b	2	0	1	∞	
D_d	∞	∞	∞	∞	D_d	4	∞	9	0	- 0 1 -
(b)	а	b	С	d	(b)	а	b	С	d	<u>ф</u>
D_b	2	0	1	∞	D_b	2	0	1	6	2 9
D_a	∞	∞	∞	∞	D_{α}	0	2	∞	4	
D_c	∞	∞	∞	∞	D_c	∞	1	0	9	- (a)(d)
$\overline{}$										
(c)	а	b	C	d	(C)	а	b	С	d	4 W
C	a ∞	b 1	C 0	d 9	$\frac{C}{D_c}$	3	b 1	c 0	d 9	-
\sim					-					-
D_c	∞	1	0	9	D_c	3	1	0	9	-
D_c D_b	∞ ∞	1 ∞	0 ∞	9 ∞	$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $	3 2	1 0	0	9 ∞	-
D_c D_b D_d	∞ ∞ ∞	1 ∞ ∞	0 ∞ ∞	9 ∞ ∞	$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $	3 2 4	1 0 ∞	0 1 9	9 ∞ 0	- - -
$\begin{array}{c} D_c \\ D_b \\ D_d \\ \hline \end{array}$	∞ ∞ ∞	1 ∞ ∞	0 ∞ ∞	9 ∞ ∞	$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $	3 2 4	1 0 ∞ b	0 1 9	9 ∞ 0	- - -
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $ $ \begin{array}{c} D_d \end{array} $	∞ ∞ ∞ a 4	1 ∞ ∞ b ∞	0 ∞ ∞ c	9 ∞ ∞ d 0	$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $	3 2 4 a 4	1 0 ∞ b	0 1 9 c	9 ∞ 0 d 0	=

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a	а	b	С	d	a	а	b	С	d	a	а	b	С	d
Da	0	2	∞	4	Da	0	2	3	4	Da	0	2	3	4
D_b	∞	∞	∞	∞	D_b	2	0	1	∞	D_b	2	0	1	6
D_d	∞	∞	∞	∞	D_d	4	∞	9	0	D_d	4	6	9	0
b	а	b	С	d	b	а	b	С	d	b	а	b	С	d
D_b	2	0	1	∞	D_b	2	0	1	6	D_b	2	0	1	6
D_a	∞	∞	∞	∞	D_{α}	0	2	∞	4	D_a	0	2	3	4
D_{C}	∞	∞	∞	∞	D_{c}	∞	1	0	9	D_{C}	3	1	0	9
(0)	a	b	С	d	(c)	a	b	С	d	(c)	а	b	С	d
D_{c}	∞	1	0	9	D_{c}	3	1	0	9	D_{c}	3	1	0	7
D_b	∞	∞	∞	∞	D_b	2	0	1	∞	D_b	2	0	1	6
D_d	∞	∞	∞	∞	D_d	4	∞	9	0	D_d	4	6	9	0
d	а	b	С	d	d	а	b	С	d	d	а	b	С	d
D_d	4	∞	9	0	D_d	4	6	9	0	D_d	4	6	7	0
D_{α}	∞	∞	∞	∞	D_{α}	0	2	∞	4	D_{a}	0	2	3	4
D_{C}	∞	∞	∞	∞	D_{c}	∞	1	0	9	D_{C}	3	1	0	9