

# Distance-Vector Routing

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- Recap on link-state routing
- Distance-vector routing
- Bellman-Ford equation
- Distance-vector algorithm
- Examples

## Recap on Routing

- Goal: each router  $u$  must be able to compute, for each other router  $v$ , the next-hop neighbor  $x$  that is on the least-cost path from  $u$  to  $v$



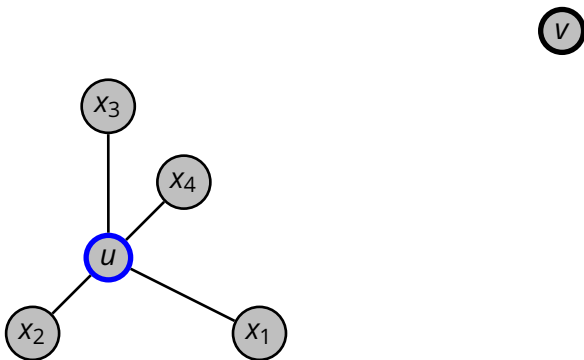
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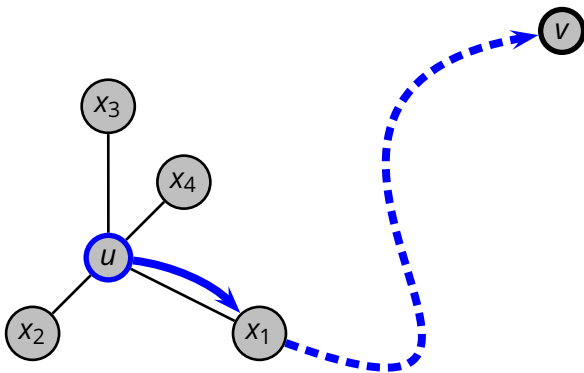
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- Routers use LSAs from other routers to compile an image of the entire network
- With a complete knowledge of the network topology, routers perform a local computation (Dijkstra's algorithm) to find the least-cost paths to every other router
- In essence
  - ▶ *broadcast transmission of topology information*
  - ▶ *global knowledge of the network*
  - ▶ *local computation*

# Changes in Link Costs

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- Routers monitor the state of their adjacent links
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- The measured costs are used to build LSAs, which are issued also at regular intervals
- Changes in link costs are propagated quickly to all routers
- Routers can then react by recomputing paths and by updating their forwarding tables accordingly
  - ▶ in fact, this “reaction” is not different from the normal behavior of the protocol

# Distance-Vector Routing



# Distance-Vector Routing

- Every router  $u$  maintains a “*distance vector*”
  - ▶  $v$  is a destination node in the network
  - ▶  $D_u[v]$  is the best known distance between  $u$  and  $v$
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- Routers exchange their distance vectors with their neighbors
- If the distance vector of a neighbor leads to a better path to some destinations, the router updates its distance vector and sends it out again to its neighbors
- After a number of iterations, *the algorithm converges to a point where every router has a minimal distance vector*

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- Local transmission of topology information
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  - ▶ router  $u$  knows its distance  $D_u[v]$  and the first step along that path
  - ▶ router  $u$  does not know about any link cost except its adjacent links
- Global computation
  - ▶ the computation is actually distributed



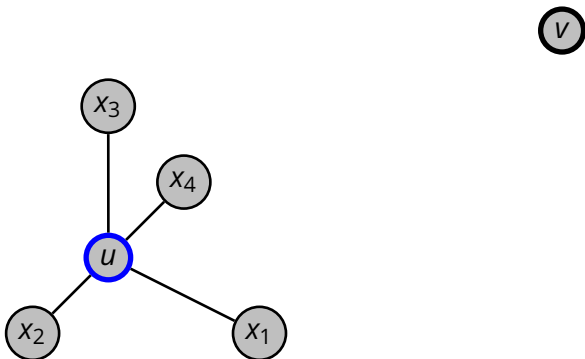


- The main idea behind the distance-vector algorithm is expressed well by the *Bellman-Ford equation*

$$D'_u[v] = \min_{x \in \text{neighbors}(u)} (c(u, x) + D_x[v])$$

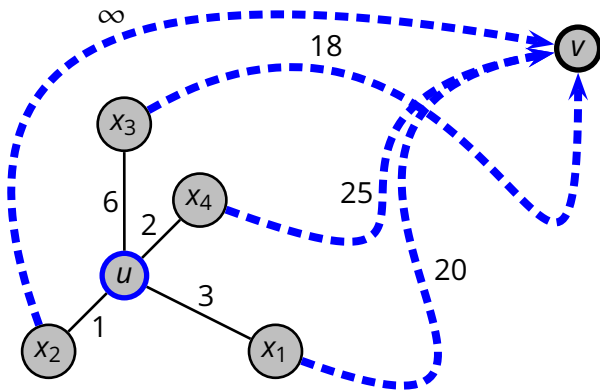
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  - ▶  $n_u[v]$ , next-hop node (neighbor of  $u$ ) on the least-cost path from  $u$  to  $v$
  - ▶  $D_x[v]$ , distance vectors of every neighbor node  $x$

# Distance-Vector Algorithm: Initialization

```
▷ Initialization
1  for  $v \in V$ 
2      do if  $v \in neighbors(u)$ 
3          then  $D_u[v] \leftarrow c(u, v)$ 
4               $n_u[v] \leftarrow v$ 
5          else  $D_u[v] \leftarrow \infty$ 
6  for  $x \in neighbors(u)$ 
7      do for  $v \in V$ 
8          do  $D_x[v] \leftarrow \infty$ 
9  send  $D_u$  to all neighbor nodes
```

# Distance-Vector Algorithm: Loop

```
1  when  $D'_x$  is received from neighbor  $x$ 
2      do  $D_x \leftarrow D'_x$ 
3          for  $v \in N$ 
4              do  $D_u[v] \leftarrow \min_{x \in neighbors(u)} (c(u, x) + D_x[v])$ 
5          if  $D_u$  was updated
6              then send  $D_u$  to all neighbor nodes

7  when link cost  $c(u, x)$  changes
8      do for  $v \in N$ 
9          do  $D_u[v] \leftarrow \min_{x \in neighbors(u)} (c(u, x) + D_x[v])$ 
10         if  $D_u$  was updated
11             then send  $D_u$  to all neighbor nodes
```

## Distance-Vector Algorithm: $D_u$ Update

▷ updating  $D_u$ :

▷  $\forall v \in N : D_u[v] \leftarrow \min_{x \in neighbors(u)} (c(u, x) + D_x[v])$

1 *updated*  $\leftarrow$  FALSE

2 **for**  $v \in N$

3     **do for**  $x \in neighbors(u)$

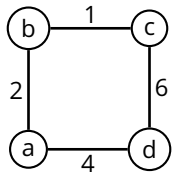
4         **do if**  $D_u[v] > c(u, x) + D_x[v]$

5             **then**  $D_u[v] \leftarrow c(u, x) + D_x[v]$

6                  $n_u[v] \leftarrow x$

7             *updated*  $\leftarrow$  TRUE

# Example



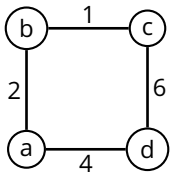
# Example

| (a)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_a$ | 0        | 2        | $\infty$ | 4        |
| $D_b$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_d$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (b)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_b$ | 2        | 0        | 1        | $\infty$ |
| $D_a$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_c$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (c)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_c$ | $\infty$ | 1        | 0        | 6        |
| $D_b$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_d$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (d)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_d$ | 4        | $\infty$ | 6        | 0        |
| $D_a$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_c$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |



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| (b)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
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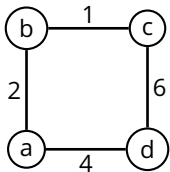
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| (a)   | a | b        | c        | d        |
|-------|---|----------|----------|----------|
| $D_a$ | 0 | 2        | <b>3</b> | 4        |
| $D_b$ | 2 | 0        | 1        | $\infty$ |
| $D_d$ | 4 | $\infty$ | 6        | 0        |

| (b)   | a        | b | c        | d        |
|-------|----------|---|----------|----------|
| $D_b$ | 2        | 0 | 1        | <b>6</b> |
| $D_a$ | 0        | 2 | $\infty$ | 4        |
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| (c)   | a        | b        | c | d        |
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| $D_c$ | <b>3</b> | 1        | 0 | 6        |
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|-------|----------|----------|----------|---|
| $D_d$ | 4        | <b>6</b> | 6        | 0 |
| $D_a$ | 0        | 2        | $\infty$ | 4 |
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| $D_d$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (b)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_b$ | 2        | 0        | 1        | $\infty$ |
| $D_a$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_c$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (c)   | a        | b        | c        | d        |
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| $D_d$ | 4 | $\infty$ | 6        | 0        |

| (b)   | a        | b | c        | d        |
|-------|----------|---|----------|----------|
| $D_b$ | 2        | 0 | 1        | <b>6</b> |
| $D_a$ | 0        | 2 | $\infty$ | 4        |
| $D_c$ | $\infty$ | 1 | 0        | 6        |

| (c)   | a        | b        | c | d        |
|-------|----------|----------|---|----------|
| $D_c$ | <b>3</b> | 1        | 0 | 6        |
| $D_b$ | 2        | 0        | 1 | $\infty$ |
| $D_d$ | 4        | $\infty$ | 6 | 0        |

| (d)   | a        | b        | c        | d |
|-------|----------|----------|----------|---|
| $D_d$ | 4        | <b>6</b> | 6        | 0 |
| $D_a$ | 0        | 2        | $\infty$ | 4 |
| $D_c$ | $\infty$ | 1        | 0        | 6 |

| (a)   | a | b | c | d |
|-------|---|---|---|---|
| $D_a$ | 0 | 2 | 3 | 4 |
| $D_b$ | 2 | 0 | 1 | 6 |
| $D_d$ | 4 | 6 | 6 | 0 |

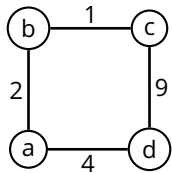
| (b)   | a | b | c | d |
|-------|---|---|---|---|
| $D_b$ | 2 | 0 | 1 | 6 |
| $D_a$ | 0 | 2 | 3 | 4 |
| $D_c$ | 3 | 1 | 0 | 6 |

| (c)   | a | b | c | d |
|-------|---|---|---|---|
| $D_c$ | 3 | 1 | 0 | 6 |
| $D_b$ | 2 | 0 | 1 | 6 |
| $D_d$ | 4 | 6 | 6 | 0 |

| (d)   | a | b | c | d |
|-------|---|---|---|---|
| $D_d$ | 4 | 6 | 6 | 0 |
| $D_a$ | 0 | 2 | 3 | 4 |
| $D_c$ | 3 | 1 | 0 | 6 |



## Example (2)



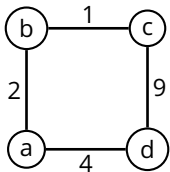
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| (a)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_a$ | 0        | 2        | $\infty$ | 4        |
| $D_b$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_d$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (b)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_b$ | 2        | 0        | 1        | $\infty$ |
| $D_a$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_c$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (c)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_c$ | $\infty$ | 1        | 0        | 9        |
| $D_b$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_d$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (d)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_d$ | 4        | $\infty$ | 9        | 0        |
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| (b)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_b$ | 2        | 0        | 1        | $\infty$ |
| $D_a$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
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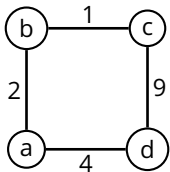
| (d)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_d$ | 4        | $\infty$ | 9        | 0        |
| $D_a$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_c$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (a)   | a | b        | c        | d        |
|-------|---|----------|----------|----------|
| $D_a$ | 0 | 2        | <b>3</b> | 4        |
| $D_b$ | 2 | 0        | 1        | $\infty$ |
| $D_d$ | 4 | $\infty$ | 9        | 0        |

| (b)   | a        | b | c        | d        |
|-------|----------|---|----------|----------|
| $D_b$ | 2        | 0 | 1        | <b>6</b> |
| $D_a$ | 0        | 2 | $\infty$ | 4        |
| $D_c$ | $\infty$ | 1 | 0        | 9        |

| (c)   | a        | b        | c | d        |
|-------|----------|----------|---|----------|
| $D_c$ | <b>3</b> | 1        | 0 | 9        |
| $D_b$ | 2        | 0        | 1 | $\infty$ |
| $D_d$ | 4        | $\infty$ | 9 | 0        |

| (d)   | a        | b        | c        | d |
|-------|----------|----------|----------|---|
| $D_d$ | 4        | <b>6</b> | 9        | 0 |
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| $D_d$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

| (b)   | a        | b        | c        | d        |
|-------|----------|----------|----------|----------|
| $D_b$ | 2        | 0        | 1        | $\infty$ |
| $D_a$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| $D_c$ | $\infty$ | $\infty$ | $\infty$ | $\infty$ |

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| $D_b$ | 2 | 0        | 1        | $\infty$ |
| $D_d$ | 4 | $\infty$ | 9        | 0        |

| (b)   | a        | b | c        | d        |
|-------|----------|---|----------|----------|
| $D_b$ | 2        | 0 | 1        | <b>6</b> |
| $D_a$ | 0        | 2 | $\infty$ | 4        |
| $D_c$ | $\infty$ | 1 | 0        | 9        |

| (c)   | a        | b        | c | d        |
|-------|----------|----------|---|----------|
| $D_c$ | <b>3</b> | 1        | 0 | 9        |
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| $D_d$ | 4        | $\infty$ | 9 | 0        |

| (d)   | a        | b        | c        | d |
|-------|----------|----------|----------|---|
| $D_d$ | 4        | <b>6</b> | 9        | 0 |
| $D_a$ | 0        | 2        | $\infty$ | 4 |
| $D_c$ | $\infty$ | 1        | 0        | 9 |

| (a)   | a | b | c | d |
|-------|---|---|---|---|
| $D_a$ | 0 | 2 | 3 | 4 |
| $D_b$ | 2 | 0 | 1 | 6 |
| $D_d$ | 4 | 6 | 9 | 0 |

| (b)   | a | b | c | d |
|-------|---|---|---|---|
| $D_b$ | 2 | 0 | 1 | 6 |
| $D_a$ | 0 | 2 | 3 | 4 |
| $D_c$ | 3 | 1 | 0 | 9 |

| (c)   | a | b | c | d        |
|-------|---|---|---|----------|
| $D_c$ | 3 | 1 | 0 | <b>7</b> |
| $D_b$ | 2 | 0 | 1 | 6        |
| $D_d$ | 4 | 6 | 9 | 0        |

| (d)   | a | b | c        | d |
|-------|---|---|----------|---|
| $D_d$ | 4 | 6 | <b>7</b> | 0 |
| $D_a$ | 0 | 2 | 3        | 4 |
| $D_c$ | 3 | 1 | 0        | 9 |