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#### **Outline**

- Recap on link-state routing
- Distance-vector routing
- Bellman-Ford equation
- Distance-vector algorithm
- Examples

■ Goal: each router *u* must be able to compute, for each other router *v*, the next-hop neighbor *x* that is on the least-cost path from *u* to *v* 



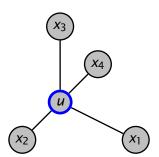
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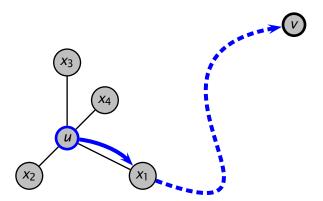


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- With a complete knowledge of the network topology, routers perform a local computation (Dijkstra's algorithm) to find the least-cost paths to every other router
- In essence
  - broadcast transmission of topology information
  - global knowledge of the network
  - local computation

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- The measured costs are used to build LSAs, which are issued also at regular intervals
- Changes in link costs are propagated quickly to all routers
- Routers can then react by recomputing paths and by updating their forwarding tables accordingly
  - in fact, this "reaction" is not different from the normal behavior of the protocol

- Every router u maintains a "distance vector"
  - v is a destination node in the network
  - $\triangleright$   $D_u[v]$  is the best known distance between u and v
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- Routers exchange their distance vectors with their neighbors
- If the distance vector of a neighbor leads to a better path to some destinations, the router updates its distance vector and sends it out again to its neighbors
- After a number of iterations, the algorithm converges to a point where every router has a minimal distance vector

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  - no broadcast protocol needed (a *local broadcast* can be useful)

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- Local knowledge of the network
  - router u knows its distance  $D_u[v]$  and the first step along that path
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- Global computation
  - the computation is actually distributed

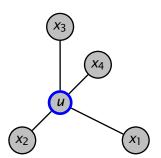
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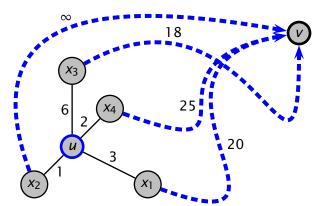
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  - $\triangleright$   $D_u[v]$ , cost of the least-cost path from u to v (distance vector)
  - n<sub>u</sub>[v], next-hop node (neighbor of u) on the least-cost path from u to v
  - ▶  $D_x[v]$ , distance vectors of every neighbor node x

#### **Distance-Vector Algorithm: Initialization**

```
▷ Initialization
    for v \in V
           do if v \in neighbors(u)
3
                  then D_u[v] \leftarrow c(u,v)
                          n_{u}[v] \leftarrow v
4
                  else D_{u}[v] \leftarrow \infty
6
    for x \in neighbors(u)
           do for v \in V
8
                     do D_x[v] \leftarrow \infty
    send D_{\mu} to all neighbor nodes
9
```

#### Distance-Vector Algorithm: Loop

```
when D'_x is received from neighbor x
           do D_x \leftarrow D_y'
               for v \in N
                    do D_u[v] \leftarrow \min_{x \in neighbors(u)} (c(u, x) + D_x[v])
 5
               if D_{\mu} was updated
 6
                  then send D_u to all neighbor nodes
     when link cost c(u, x) changes
 8
           do for v \in N
                    do D_{u}[v] \leftarrow \min_{x \in neighbors(u)} (c(u, x) + D_{x}[v])
 9
10
               if D_{\mu} was updated
11
                  then send D_{\mu} to all neighbor nodes
```

### Distance-Vector Algorithm: *Du* Update



a	a	b	С	d
Da	0	2	$\infty$	4
$D_a$ $D_b$	$\infty$	$\infty$	$\infty$	$\infty$
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$
b	a	b	С	d
$D_b$ $D_a$	2	0	1	$\infty$
$D_a$	$\infty$	$\infty$	$\infty$	$\infty$
$D_c$	$\infty$	$\infty$	$\infty$	$\infty$
(c)	a	b	С	d
$\sim$				
$\sim$	∞	1	0	6
$D_c$ $D_b$	∞ ∞	1 ∞	0 ∞	6 ∞
$\sim$		-	-	
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $	∞	∞	∞	$\infty$
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $	∞ ∞	∞ ∞	∞ ∞	∞ ∞
D <sub>c</sub> D <sub>b</sub> D <sub>d</sub>	∞ ∞ a	∞ ∞ b	∞ ∞	∞ ∞ d



a	a	b	С	d	a	a
Da	0	2	$\infty$	4	Da	0
$D_b$	$\infty$	$\infty$	$\infty$	$\infty$	$D_b$	2
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$	$D_d$	4
b	a	b	С	d	b	a
$D_b$	2	0	1	$\infty$	$D_b$	2
$D_a$	$\infty$	$\infty$	$\infty$	$\infty$	$D_a$	0
$D_c$	$\infty$	$\infty$	$\infty$	$\infty$	$D_c$	ox.
C	a	b	С	d	<u>C</u>	a
	a ∞	b 1	c 0	d 6	<u>C</u>	
$D_c$ $D_b$					$C$ $D_c$ $D_b$	3
$D_c$	∞	1	0	6	<u>C</u>	
D <sub>c</sub> D <sub>b</sub> D <sub>d</sub>	∞ ∞	1 ∞	0 ∞	6 ∞	$C$ $D_c$ $D_b$	3 2 4
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $ $ \begin{array}{c} D_d \end{array} $	& & & &	1 ∞ ∞	0 ∞ ∞	6 ∞ ∞	$ \begin{array}{c c} \hline C \\ D_c \\ D_b \\ D_d \end{array} $	3 2 4
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $ $ \begin{array}{c} D_d \\ D_d \\ D_a \end{array} $	∞ ∞ ∞	1 ∞ ∞	0 ∞ ∞	6 ∞ ∞	$ \begin{array}{c c} \hline C \\ D_c \\ D_b \\ D_d \\ \hline D_d \\ D_a \end{array} $	3 2 4
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $ $ \begin{array}{c} D_d \end{array} $	∞ ∞ ∞ a 4	1 ∞ ∞ b ∞	0 ∞ ∞ c 6	6 ∞ ∞ d 0	$ \begin{array}{c c} \hline C \\ D_c \\ D_b \\ D_d \end{array} $	3 2 4 a

(a)	a	b	C	d	
Da	0	2	3	4	-
$D_b$	2	0	1	$\infty$	
D <sub>a</sub> D <sub>b</sub> D <sub>d</sub>	4	$\infty$	6	0	_
b	a	b	С	d	(
$D_b$	2	0	1	6	-
$D_a$	0	2	$\infty$	4	•
D <sub>b</sub> D <sub>a</sub> D <sub>c</sub>	$\infty$	1	0	6	_ (
(0)	a	b	С	d	- '
$D_c$	3	1	0	6	
D,	_	_	-		
Db	2	0	1	$\infty$	
$C$ $D_c$ $D_b$ $D_d$	4	0 ∞	1 6	0	_
d		-			=
	4	∞	6	0	=

6



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(a)	a	b	C	d	(a)	a	b	C	d	(a)	a	b	C	d
$D_a$	0	2	$\infty$	4	Da	0	2	3	4	Da	0	2	3	4
$D_b$	$\infty$	$\infty$	$\infty$	$\infty$	$D_b$	2	0	1	$\infty$	$D_b$	2	0	1	6
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$	$D_d$	4	∞	6	0	$D_d$	4	6	6	0
b	a	b	С	d	b	a	b	С	d	b	a	b	С	d
$D_b$	2	0	1	$\infty$	$D_b$	2	0	1	6	$D_b$	2	0	1	6
$D_a$	$\infty$	$\infty$	$\infty$	$\infty$	$D_a$	0	2	$\infty$	4	$D_a$	0	2	3	4
$D_c$	8	$\infty$	$\infty$	$\infty$	$D_c$	$\infty$	1	0	6	$D_c$	3	1	0	6
(C)	a	b	С	d	(0)	a	b	С	d	(C)	a	b	С	d
$D_c$	$\infty$	1	0	6	$D_c$	3	1	0	6	$D_c$	3	1	0	6
$D_b$	$\infty$	$\infty$	$\infty$	$\infty$	$D_b$	2	0	1	$\infty$	$D_b$	2	0	1	6
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$	$D_d$	4	∞	6	0	$D_d$	4	6	6	0
d	a	b	С	d	d	a	b	С	d	d	a	b	С	d
$D_d$	4	$\infty$	6	0	$D_d$	4	6	6	0	$D_d$	4	6	6	0
$D_a$	$\infty$	$\infty$	$\infty$	$\infty$	$D_a$	0	2	$\infty$	4	$D_a$	0	2	3	4
$D_c$	$\infty$	$\infty$	$\infty$	$\infty$	$D_c$	$\infty$	1	0	6	$D_c$	3	1	0	6



(a)	a	b	С	d
Da	0	2	$\infty$	4
D <sub>a</sub> D <sub>b</sub>	$\infty$	$\infty$	$\infty$	$\infty$
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$
b	a	b	С	d
$D_b$ $D_a$	2	0	1	$\infty$
$D_a$	$\infty$	$\infty$	$\infty$	$\infty$
$D_c$	$\infty$	$\infty$	$\infty$	$\infty$
<u>c</u>	a	b	С	d
C				
=	a	b	С	d
C	a ∞	b 1	<b>c</b>	d 9
С D <sub>c</sub> D <sub>b</sub>	a ∞ ∞	b 1 ∞	c 0 ∞	d 9 ∞
D <sub>c</sub> D <sub>b</sub> D <sub>d</sub>	a ∞ ∞ ∞	b 1 ∞ ∞	C 0 ∞ ∞	d 9 ∞ ∞
D <sub>c</sub> D <sub>b</sub> D <sub>d</sub>	a ∞ ∞ ∞	b 1 ∞ ∞	c 0 ∞ ∞	d 9 ∞ ∞



(a)	a	b	С	d	(
Da	0	2	$\infty$	4	D
$D_b$	∞	$\infty$	$\infty$	$\infty$	D
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$	D
(b)	a	b	С	d	
$D_b$	2	0	1	$\infty$	D
$D_a$	$\infty$	$\infty$	$\infty$	$\infty$	D
$D_c$	∞	$\infty$	$\infty$	$\infty$	D
<u>C</u>	a	b	С	d	(
$D_c$	a ∞	b 1	c 0	d 9	D
$D_c$ $D_b$					D
$D_c$	∞	1	0	9	
$D_c$ $D_b$ $D_d$	∞ ∞	1 ∞	0 ∞	9 ∞	
$D_c$ $D_b$ $D_d$	⊗ ⊗ ⊗	1 ∞ ∞	0 ∞ ∞	9 ∞ ∞	D
$ \begin{array}{c} D_c \\ D_b \\ D_d \end{array} $ $ \begin{array}{c} D_d \\ D_d \\ D_a \end{array} $	∞ ∞ ∞	1 ∞ ∞	0 ∞ ∞	9 ∞ ∞	
$D_c$ $D_b$ $D_d$	∞ ∞ ∞ a 4	1 ∞ ∞ b ∞	0 ∞ ∞ c 9	9 ∞ ∞ d 0	

a	a	b	С	d	-
Da	0	2	3	4	-
$D_b$	2	0	1	$\infty$	
D <sub>a</sub> D <sub>b</sub> D <sub>d</sub>	4	$\infty$	9	0	_
b	a	b	С	d	(
$D_b$	2	0	1	6	-
$D_a$	0	2	$\infty$	4	
D <sub>b</sub> D <sub>a</sub> D <sub>c</sub>	$\infty$	1	0	9	_
D <sub>c</sub> D <sub>b</sub> D <sub>d</sub>	a	b	С	d	-
$D_c$	3	1	0	9	•
$D_b$	2	0	1	$\infty$	
$D_d$	4	$\infty$	9	0	_
d	a	b	С	d	•
$D_d$ $D_a$	4	6	9	0	
$D_{\alpha}$	0	2	$\infty$	4	



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(a)	a	b	C	d	(a)	a	b	C	d	(a)	a	b	C	d
$D_a$	0	2	$\infty$	4	Da	0	2	3	4	Da	0	2	3	4
$D_b$	∞	$\infty$	$\infty$	$\infty$	$D_b$	2	0	1	$\infty$	$D_b$	2	0	1	6
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$	$D_d$	4	$\infty$	9	0	$D_d$	4	6	9	0
b	a	b	С	d	b	a	b	С	d	b	a	b	С	d
$D_b$	2	0	1	$\infty$	$D_b$	2	0	1	6	$D_b$	2	0	1	6
$D_a$	∞	$\infty$	$\infty$	$\infty$	$D_a$	0	2	$\infty$	4	$D_a$	0	2	3	4
$D_c$	$\infty$	$\infty$	$\infty$	$\infty$	$D_c$	$\infty$	1	0	9	$D_c$	3	1	0	9
(c)	a	b	С	d	(c)	a	b	С	d	(C)	a	b	С	d
$D_c$	∞	1	0	9	$D_c$	3	1	0	9	$D_c$	3	1	0	7
$D_b$	∞	$\infty$	$\infty$	$\infty$	$D_b$	2	0	1	$\infty$	$D_b$	2	0	1	6
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$	$D_d$	4	$\infty$	9	0	$D_d$	4	6	9	0
(d)	a	b	С	d	d	a	b	С	d	d	a	b	С	d
			9	0	$D_d$	4	6	9	0	$D_d$	4	6	7	0
$D_d$	4	$\infty$	9	U	OI .									
$\overline{}$	4 ∞	∞	∞	∞	$D_a$	0	2	$\infty$	4	$D_a$	0	2	3	4