

# Distance-Vector Routing

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- Recap on link-state routing
- Distance-vector routing
- Bellman-Ford equation
- Distance-vector algorithm
- Examples

- Goal: each router  $u$  must compute, for every other router  $v$ , the next-hop neighbor  $x$  that is on the least-cost path from  $u$  to  $v$



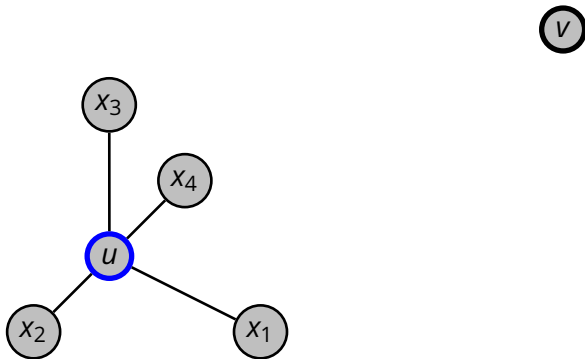
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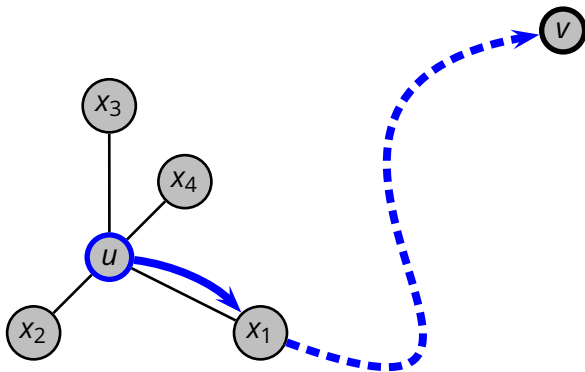
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- With a complete knowledge of the network topology, routers perform a local computation (Dijkstra's algorithm) to find the least-cost paths to every other router
- In essence
  - ▶ *broadcast transmission of topology information*
  - ▶ *global knowledge of the network*
  - ▶ *local computation*

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- The measured costs are used to build LSAs, which are issued also at regular intervals
- Changes in link costs are propagated quickly to all routers
- Routers can then react by recomputing paths and by updating their forwarding tables accordingly
  - ▶ in fact, this “reaction” is not different from the normal behavior of the protocol

# Distance-Vector Routing



- Every router  $u$  maintains a “*distance vector*”
  - ▶  $v$  is a destination node in the network
  - ▶  $D_u[v]$  is the best known distance between  $u$  and  $v$
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- Routers exchange their distance vectors with their neighbors
- If the distance vector of a neighbor leads to a better path to some destinations, the router updates its distance vector and sends it out again to its neighbors
- After a number of iterations, *the algorithm converges to a point where every router has a minimal distance vector*

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- Local transmission of topology information
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- Global computation
  - ▶ the computation is actually distributed



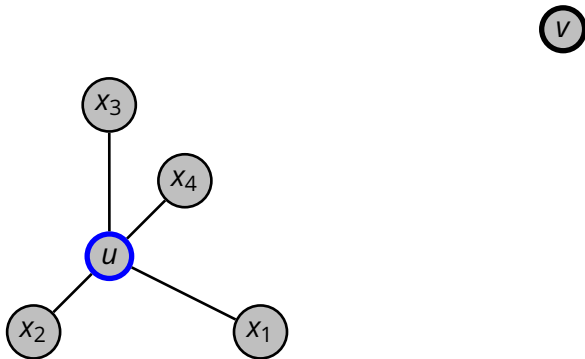


- The main idea behind the distance-vector algorithm is expressed well by the *Bellman-Ford equation*

$$D'_u[v] = \min_{x \in \text{neighbors}(u)} (c(u, x) + D_x[v])$$

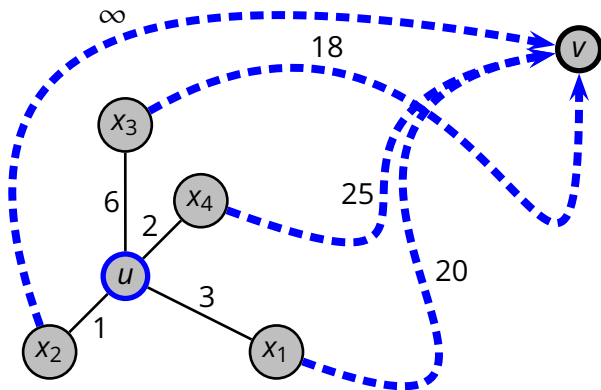
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  - ▶  $n_u[v]$ , next-hop node (neighbor of  $u$ ) on the least-cost path from  $u$  to  $v$
  - ▶  $D_x[v]$ , distance vectors of every neighbor node  $x$

## Distance-Vector Algorithm: Initialization

```
▷ Initialization
1 for  $v \in V$ 
2   do if  $v \in neighbors(u)$ 
3     then  $D_u[v] \leftarrow c(u, v)$ 
4          $n_u[v] \leftarrow v$ 
5     else  $D_u[v] \leftarrow \infty$ 
6 for  $x \in neighbors(u)$ 
7   do for  $v \in V$ 
8     do  $D_x[v] \leftarrow \infty$ 
9 send  $D_u$  to all neighbor nodes
```

## Distance-Vector Algorithm: Loop

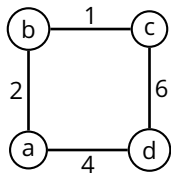
```
1  when  $D'_x$  is received from neighbor  $x$ 
2      do  $D_x \leftarrow D'_x$ 
3          for  $v \in N$ 
4              do  $D_u[v] \leftarrow \min_{x \in \text{neighbors}(u)} (c(u, x) + D_x[v])$ 
5          if  $D_u$  was updated
6              then send  $D_u$  to all neighbor nodes

7  when link cost  $c(u, x)$  changes
8      do for  $v \in N$ 
9          do  $D_u[v] \leftarrow \min_{x \in \text{neighbors}(u)} (c(u, x) + D_x[v])$ 
10         if  $D_u$  was updated
11             then send  $D_u$  to all neighbor nodes
```

## Distance-Vector Algorithm: $D_u$ Update

```
▷ updating  $D_u$ :  
▷  $\forall v \in N : D_u[v] \leftarrow \min_{x \in neighbors(u)} (c(u, x) + D_x[v])$   
1  $updated \leftarrow FALSE$   
2 for  $v \in N$   
3     do for  $x \in neighbors(u)$   
4         do if  $D_u[v] > c(u, x) + D_x[v]$   
5             then  $D_u[v] \leftarrow c(u, x) + D_x[v]$   
6                  $n_u[v] \leftarrow x$   
7                  $updated \leftarrow TRUE$ 
```

# Example



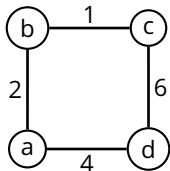
# Example

(a)	a	b	c	d
$D_a$	0	2	$\infty$	4
$D_b$	$\infty$	$\infty$	$\infty$	$\infty$
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$

(b)	a	b	c	d
$D_b$	2	0	1	$\infty$
$D_a$	$\infty$	$\infty$	$\infty$	$\infty$
$D_c$	$\infty$	$\infty$	$\infty$	$\infty$

(c)	a	b	c	d
$D_c$	$\infty$	1	0	6
$D_b$	$\infty$	$\infty$	$\infty$	$\infty$
$D_d$	$\infty$	$\infty$	$\infty$	$\infty$

(d)	a	b	c	d
$D_d$	4	$\infty$	6	0
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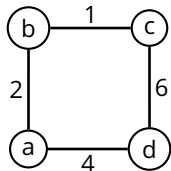
(b)	a	b	c	d
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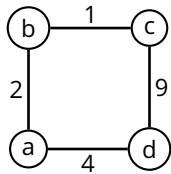
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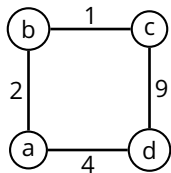
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(d)	a	b	c	d
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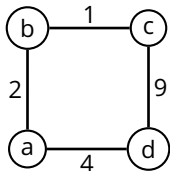
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(c)	a	b	c	d
$D_c$	3	1	0	<b>7</b>
$D_b$	2	0	1	6
$D_d$	4	6	9	0

(d)	a	b	c	d
$D_d$	4	$\infty$	9	0
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$D_d$	4	6	<b>7</b>	0
$D_a$	0	2	3	4
$D_c$	3	1	0	9